

Statistical physics for the modeling of non-equilibrium metallic alloys driven by irradiation

DE LA RECHERCHE À L'INDUSTRIE

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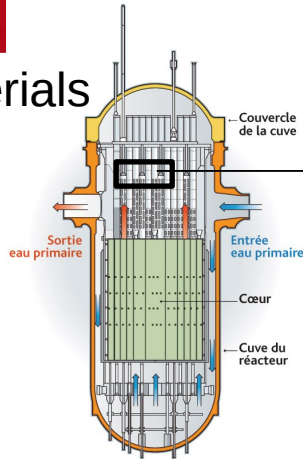
2Ecole Mines St Etienne, France

3KTH, Stockholm, Sweden

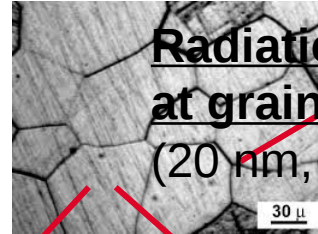
European Commission funded Enlargement workshop, KYIV, June 2017,

Irradiation damage in steels

Structural materials
Of nuclear
reactors



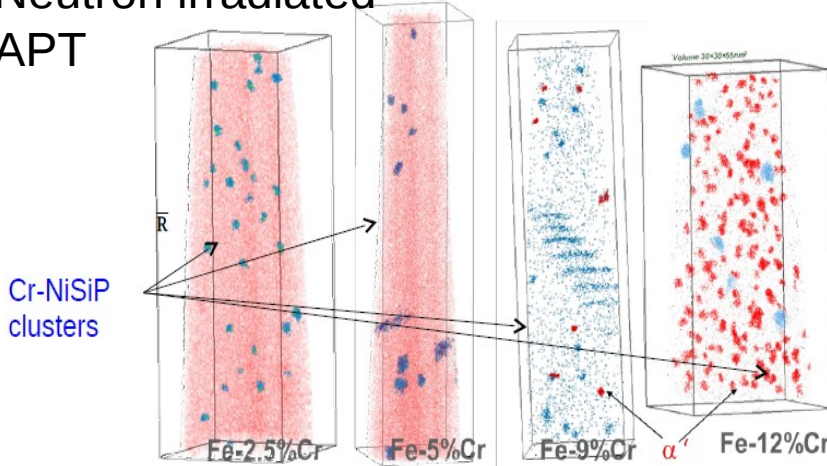
↓ ↓ ↓ irradiation



Radiation induced Segregation at grain boundaries
(20 nm, 10pa) → IASCC

Solute clustering in ferritic steels

Neutron irradiated
APT

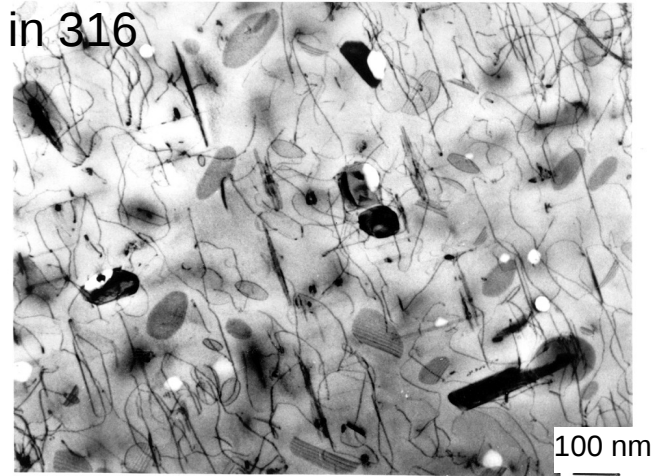


V. Kuksenko, PhD (2011); V. Kuksenko, C. Pareige, P. Pareige, J. Nucl. Mater. 432 (2013) 160

→ hardenning, embrittlement

Radiation damage
cavities, dislocation loops, etc.

TEM in 316



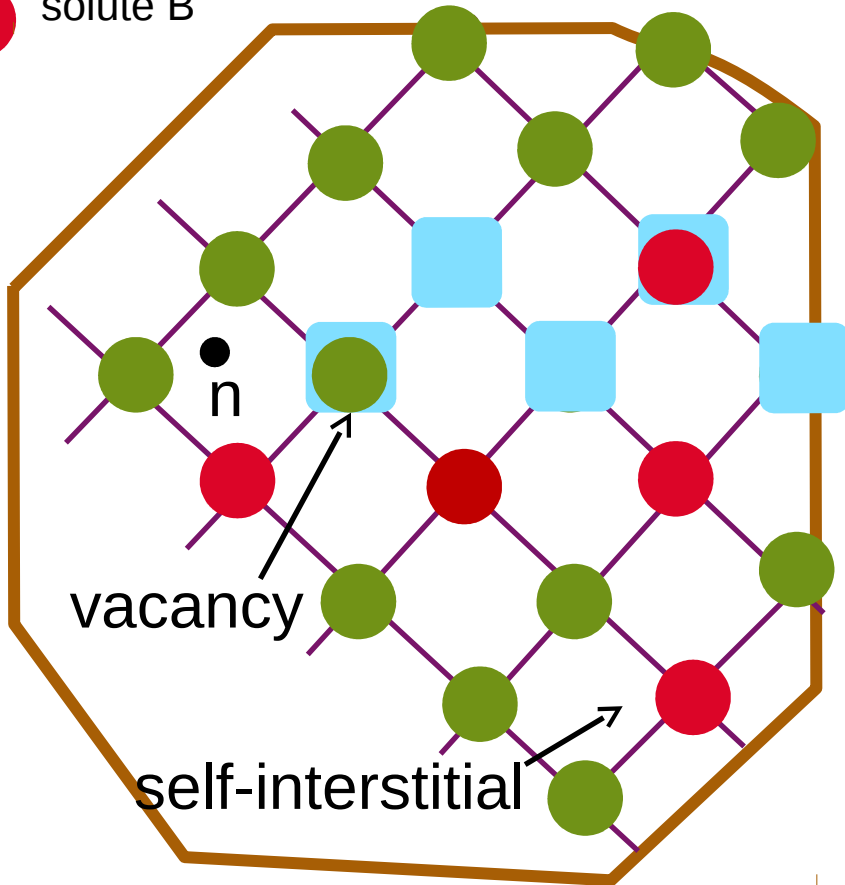
SA 316 irradiated in EBR-II to 1.9×10^{26} n/m² at 580 °C

→ embrittlement, swelling, etc.

Swelling, deformation, degradation of corrosion resistance and mechanical properties

Flux coupling

- species A
- solute B



Mechanism of radiation induced segregation:

- ✓ Point defect (PD) driving force: elimination of PD at sinks
- ✓ Flux coupling between PD and atoms

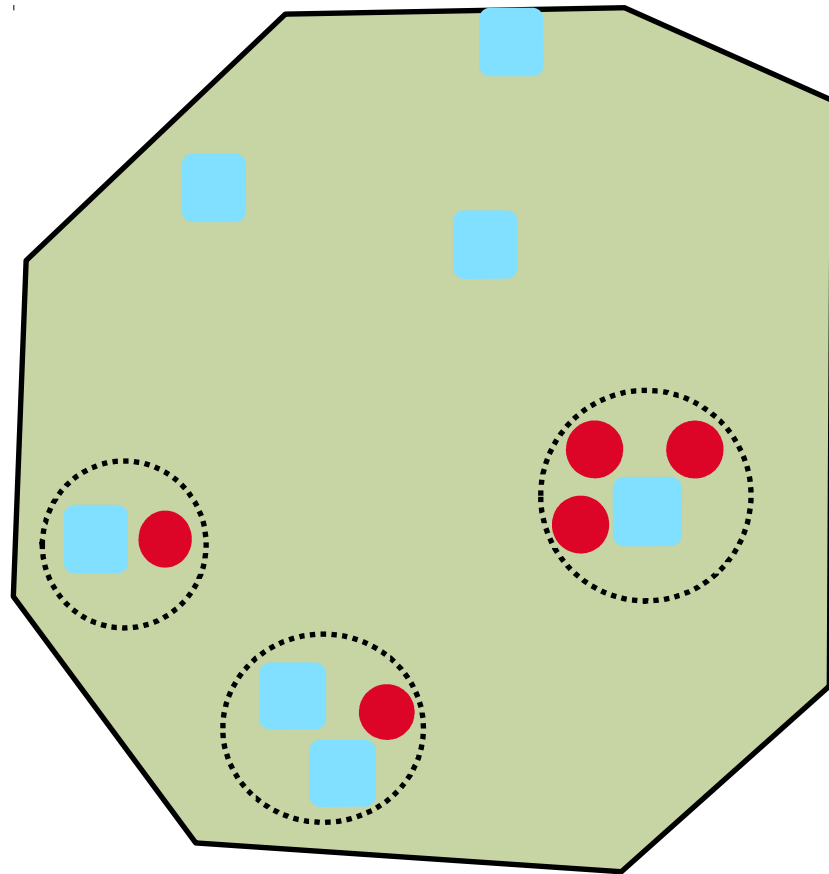
Other phenomena involving a net flow of vacancies and potential flux couplings: Quenching, diffusion creep, sintering, carburization, oxidation, nitration, etc.

Mechanisms of solute clustering

- ✓ Point defect driving force: clustering of PD (cavity, dislocation loop, C15, etc.) + Solute segregation due to flux coupling
- ✓ Solute driving force: Phase transformation and formation of a new phase

Mechanisms of precipitate dissolution

- ✓ Dynamic phase diagram
- ✓ Ballistic mixing



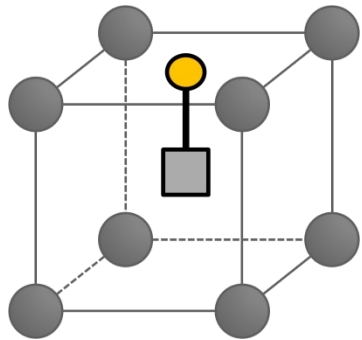
1. **Dynamic Phase Diagram of Fe(C,N,O)**

- a) Vacancy-solute cluster binding energies
- b) Solubility limits with respect to vacancy supersaturation
- c) Vacancy induced dissolution versus ballistic mixing

2. **Radiation Induced Segregation in Fe(X) (X=C,N,O,metal)**

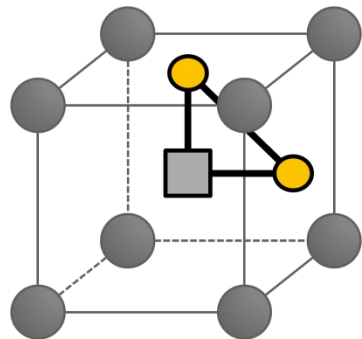
- a) Vacancy-solute cluster transport coefficients
- b) A multi-scale computation of the phenomenological coefficients L_{ij}
- c) RIS in Fe(X=C,N,O or a transition metal) alloys

DFT calculations suggest strong binding energies between X and V



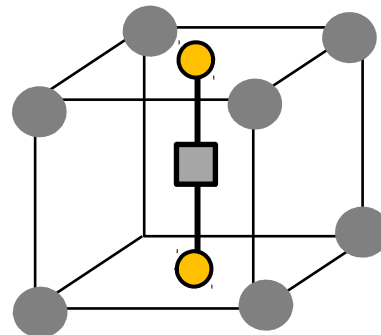
<i>E_{bt}</i> (V-X) (eV)	
X = C	0,41 - 0,65
X = N	0,71 - 0,92
X = O	1,41 - 1,69

*[Domain04;Fu08;Paxton13;
Förs t06;Jourdan11;
Ohnuma09;Fu07;Jiang09]*



***E_{bt}*(VC₂)=1.18**

eV

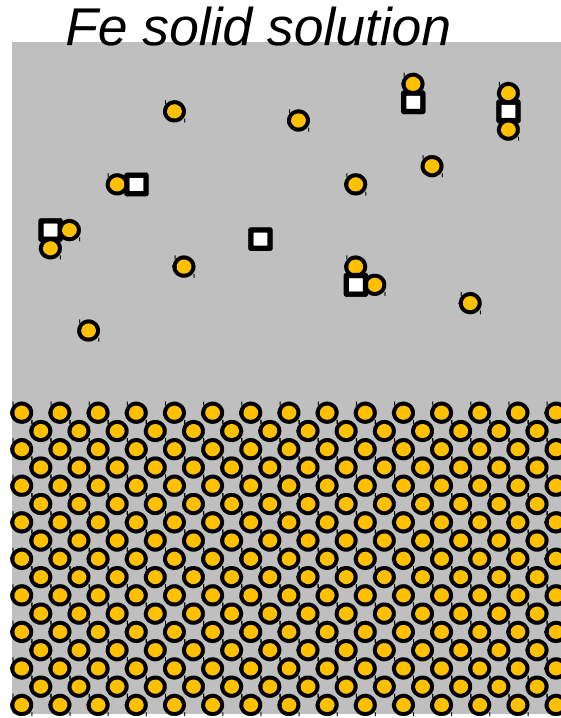


***E_{bt}*(VO₂)=3 eV**

Concentration of mixed point defect-interstitial clusters might be large

Dynamic solubility limit from a constrained chemical potential

Two phase system



Ordered compound $FepXq$

(infinite reservoir of X)

Solute chemical potential μ_X

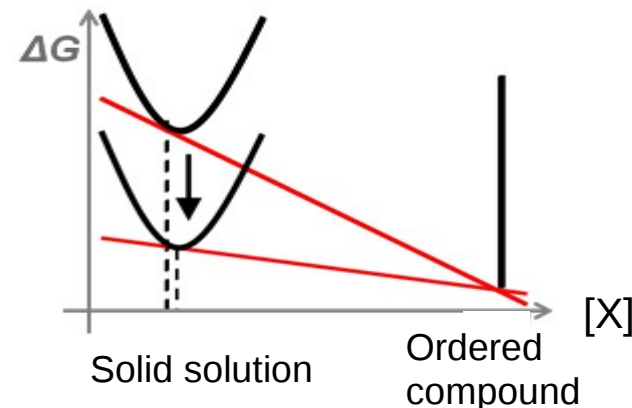
Average solute energy in a given phase

$$\mu_X \sim E[X \in Fe] - E[X \in Fe_p X_q]$$

Function of the supersaturation [V] and Cluster binding free energies

The ordered compound is assumed perfect. $E = \text{constant}$, deduced from thermodynamic database.

Shift of the solubility limit



Statistical physics to average over various clusters and cluster configurations:

[Domb 60]

[Ducastelle 91]

Low-temperature expansions (LTE)

Grand potential

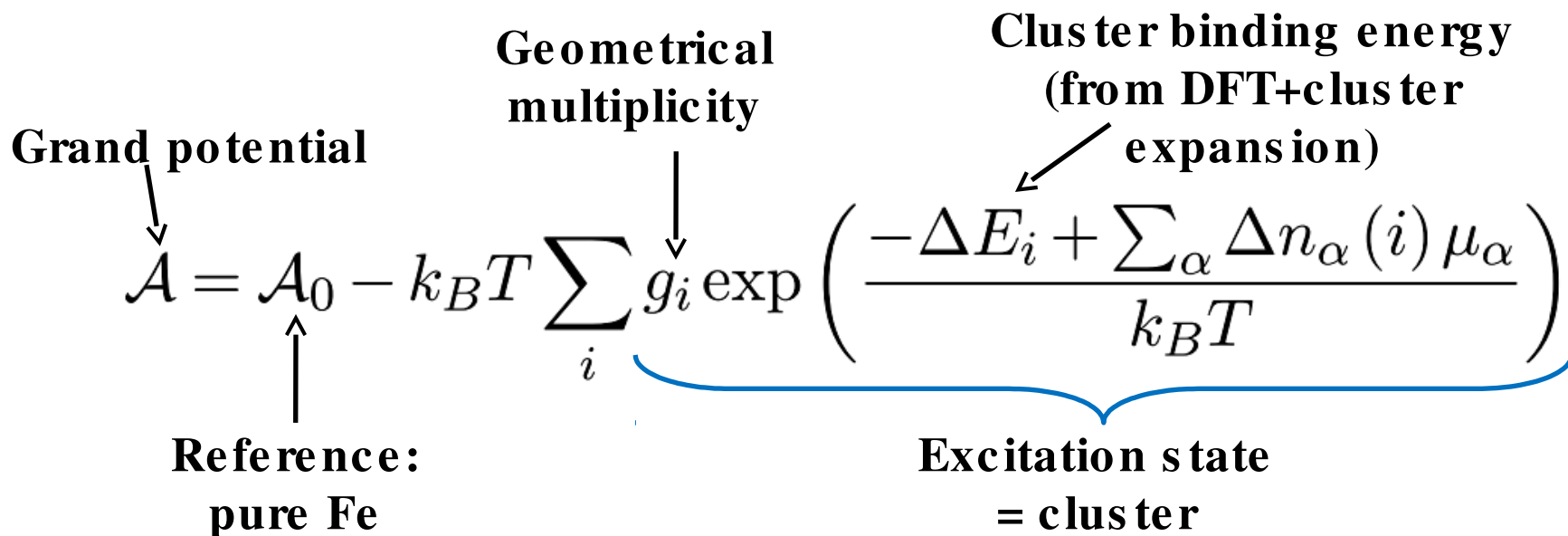
$$\mathcal{A} = \mathcal{A}_0 - k_B T \sum_i g_i \exp \left(\frac{-\Delta E_i + \sum_{\alpha} \Delta n_{\alpha}(i) \mu_{\alpha}}{k_B T} \right)$$

Reference: pure Fe

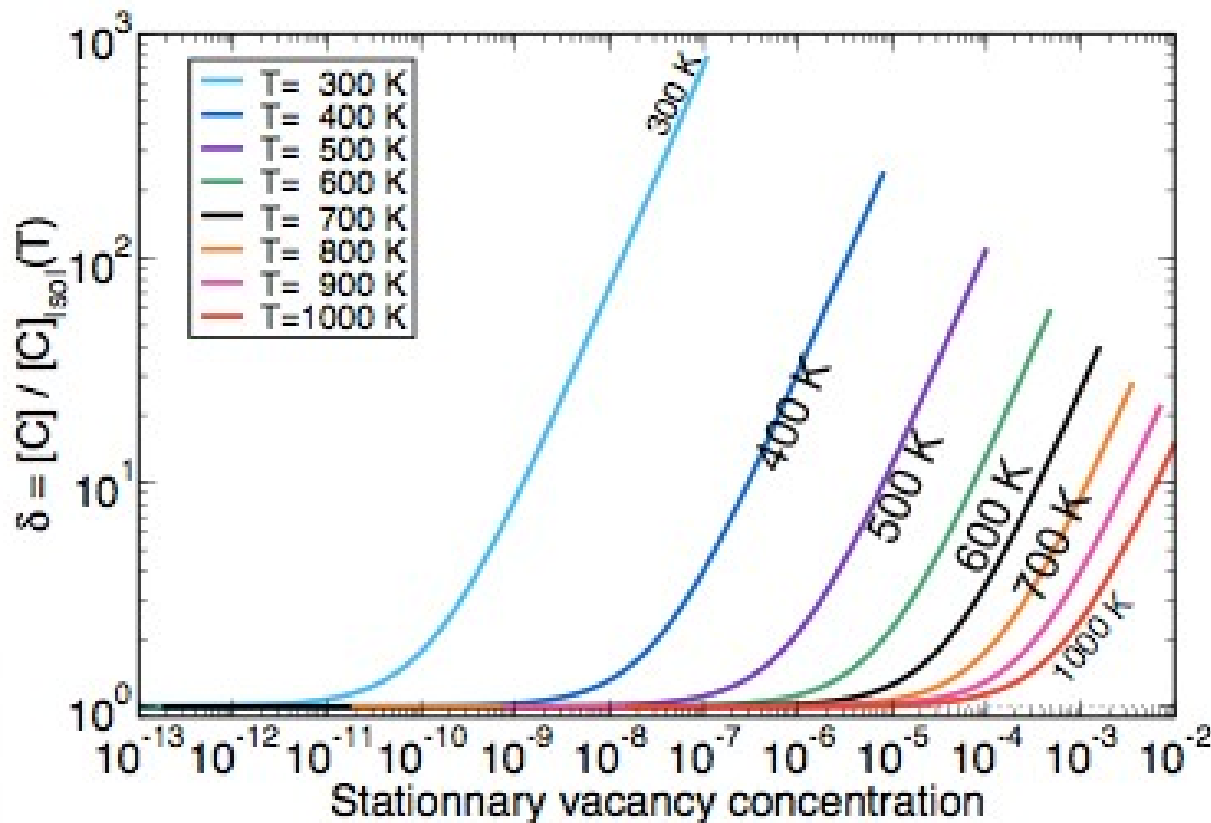
Geometrical multiplicity

Cluster binding energy (from DFT+cluster expansion)

Excitation state = cluster



Irradiation modeled by a constant vacancy supersaturation
(steady-state and local equilibrium assumption)

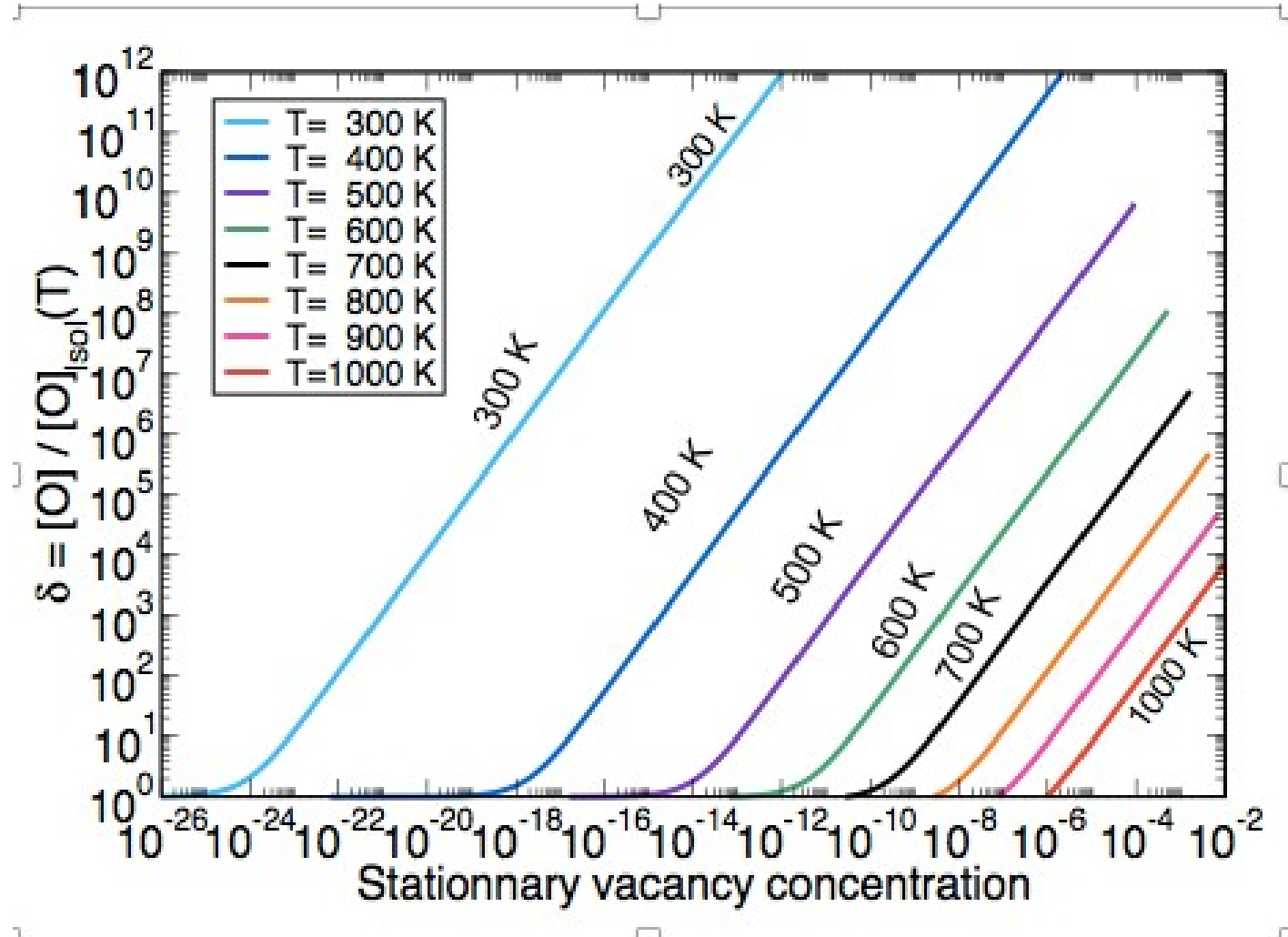


- ✓ Good agreement with AKMC simulations
- ✓ At low $[V]$, the solubility limit is the equil. one
- ✓ linear trend of d because a single cluster dominates

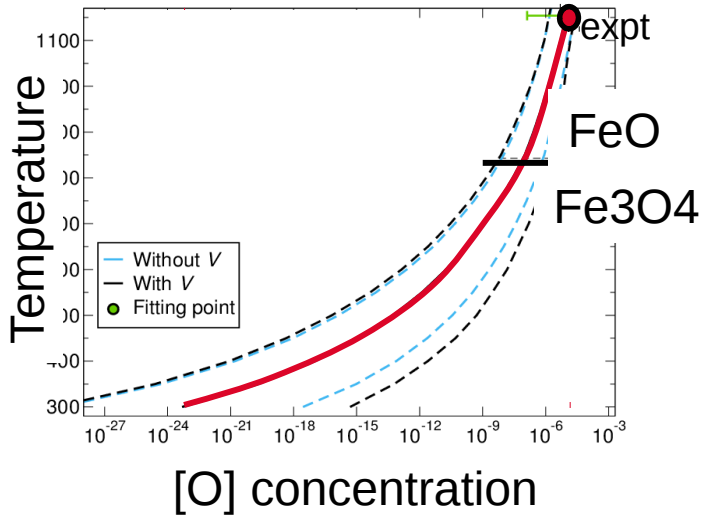
*T. Schuler et al.,
PRB 95 (2017) 014113

Dynamic solute solubility limit of N & O under irradiation

✓ Small amount of PD is required to increase the solubility limit by several orders of magnitude.

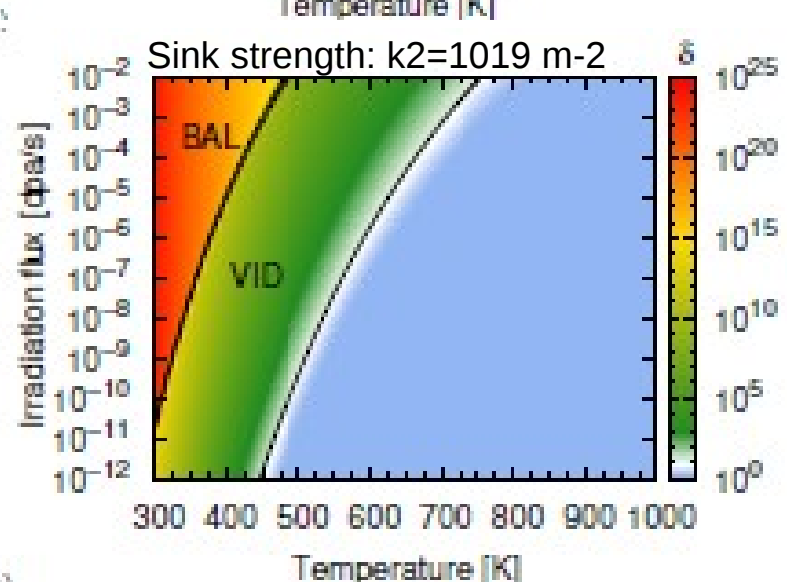
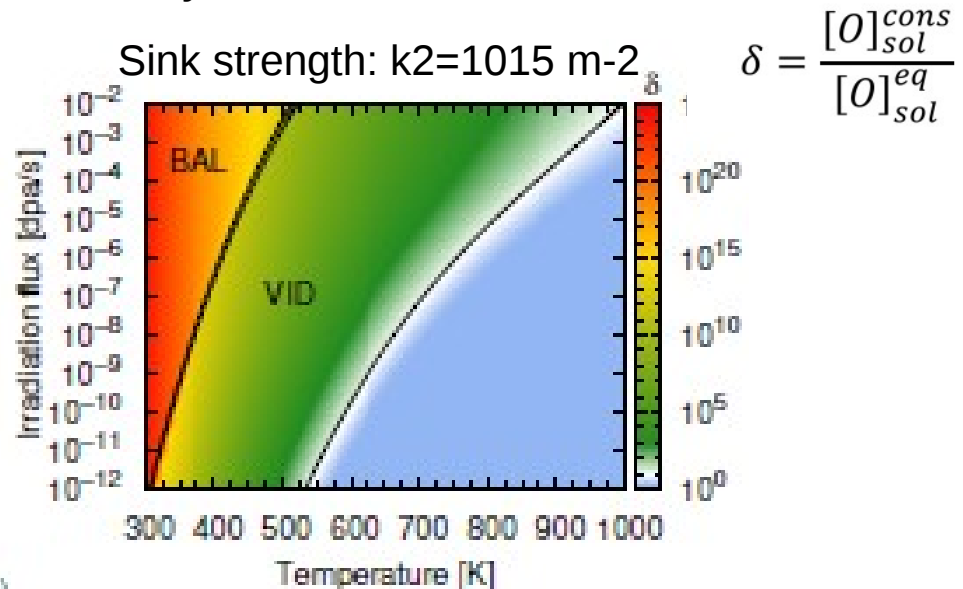


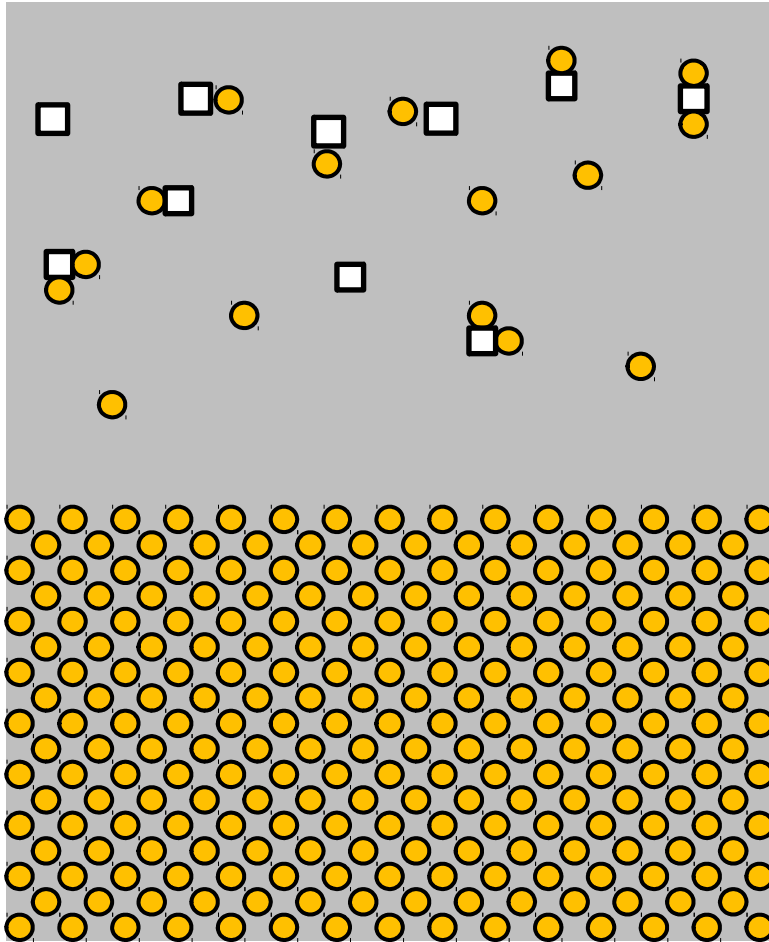
Equilibrium phase diagram



- ✓ Ballistic mixing is dominant at low T and high flux
- ✓ Vacancy induced dissolution is dominant at intermediate flux and T
- ✓ This mechanism should be considered in ODS steels

Solubility limit increase with flux and T



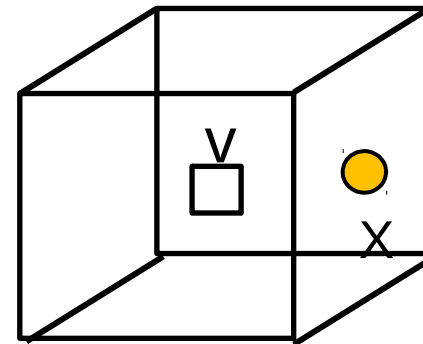
Fe solid solution*Ordered compound Fe p X q*

sign and amplitude of the flux coupling?

or

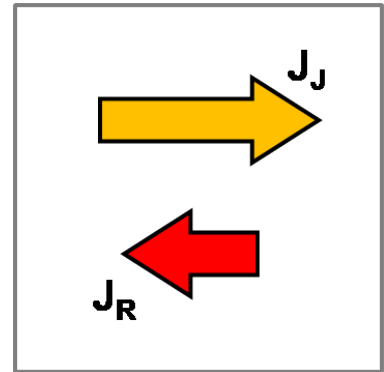
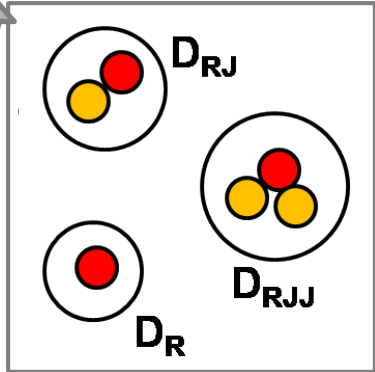
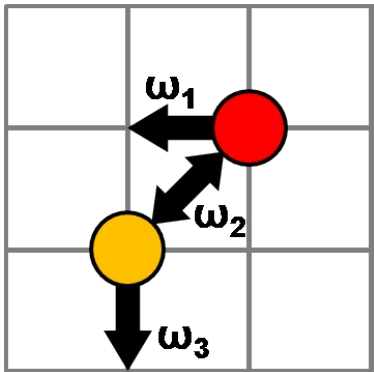
$$\square \quad \begin{aligned} J_X &= -L_{XV} \nabla \mu_V - L_{XX} \nabla \mu_X \\ J_V &= -L_{VV} \nabla \mu_V - L_{XV} \nabla \mu_X \end{aligned}$$

Lij from the atomic jump frequencies



Computation based on the SCMF theory

$$\{\omega_{p \rightarrow q}\} \quad \begin{pmatrix} L_{VV}^{eq}(c_i) & L_{VX}^{eq}(c_i) \\ L_{XV}^{eq}(c_i) & L_{XX}^{eq}(c_i) \end{pmatrix} \quad \begin{pmatrix} L_{VV} & L_{VX} \\ L_{XV} & L_{XX} \end{pmatrix}$$



DFT+SCMF

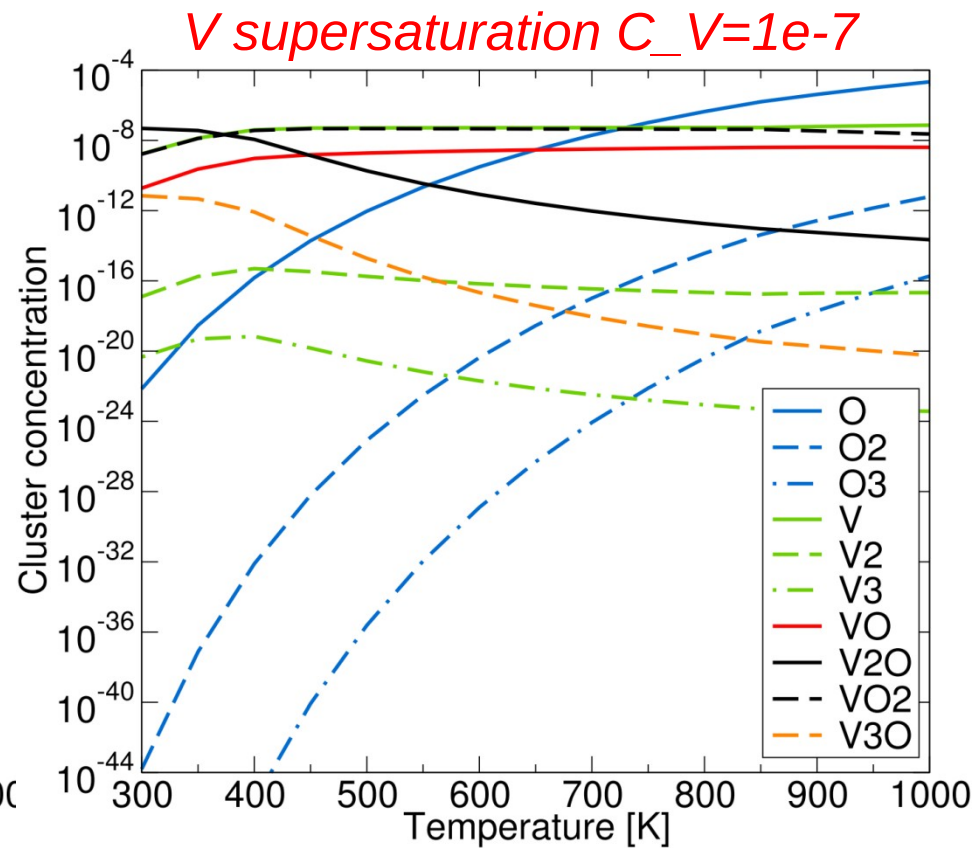
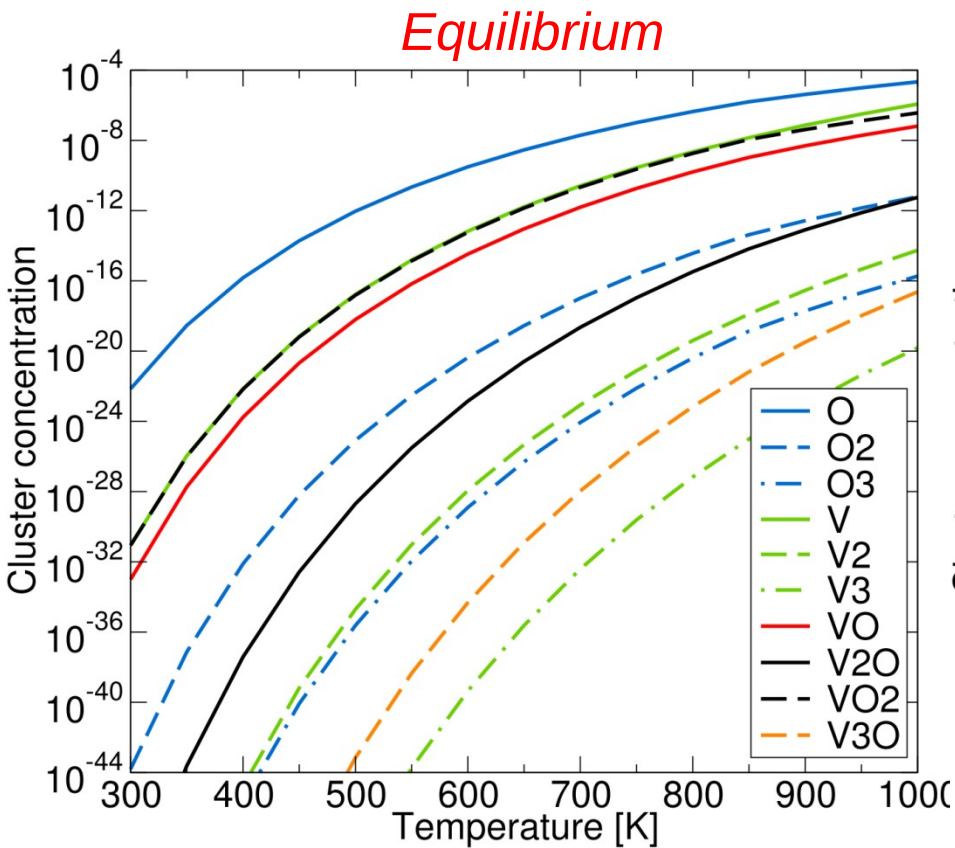
$$L_{\alpha\beta} = \sum_{c_i} [c_i] L_{\alpha\beta}^{eq}(c_i)$$

*T. Schuler et al., DIMAT 2017 - Haifa, Israel

Lattice cluster expansion based on DFT calculations

Low temperature expansion

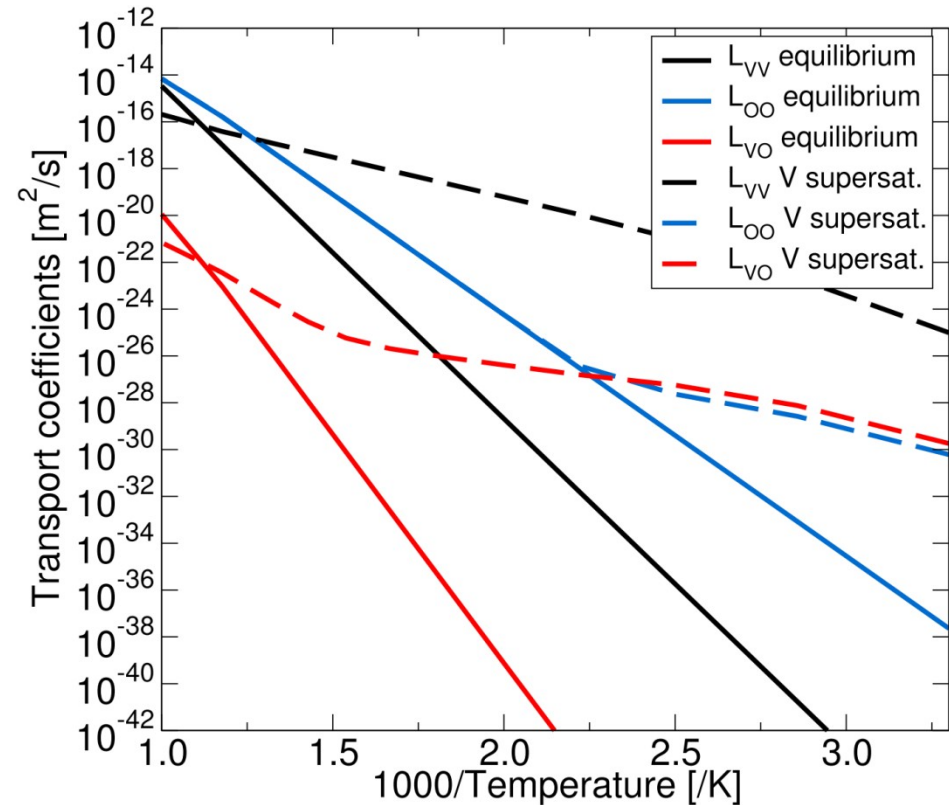
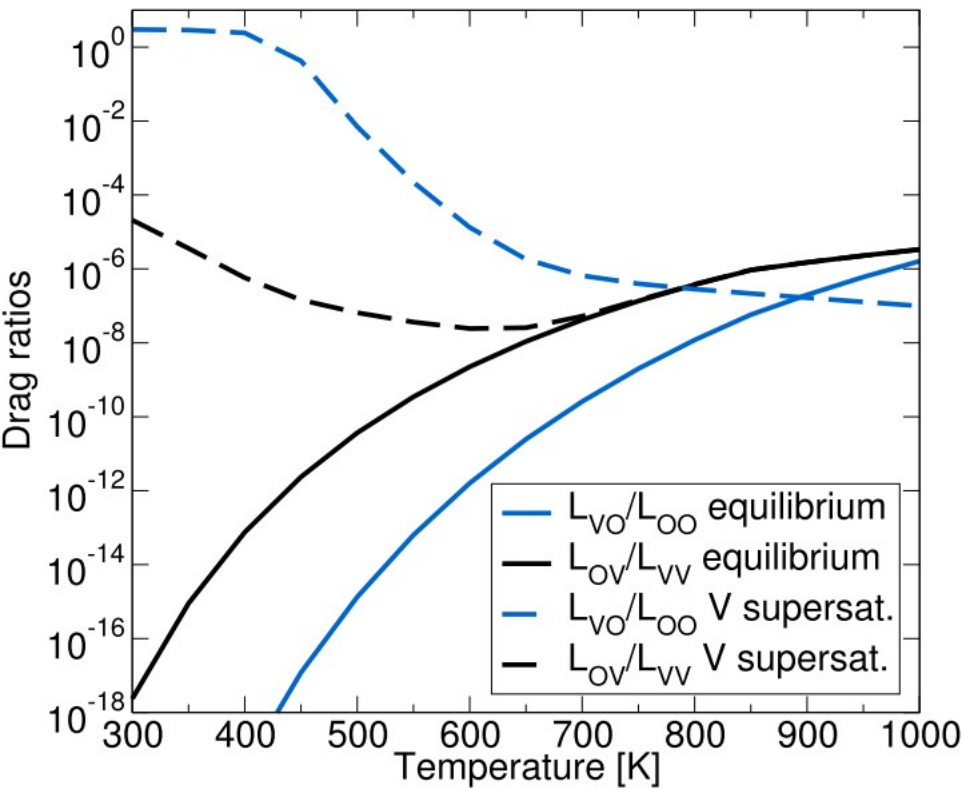
Barouh et al.
Phys. Rev B 90,
054112 (2014)



Cluster distributions + cluster transport coefficients:

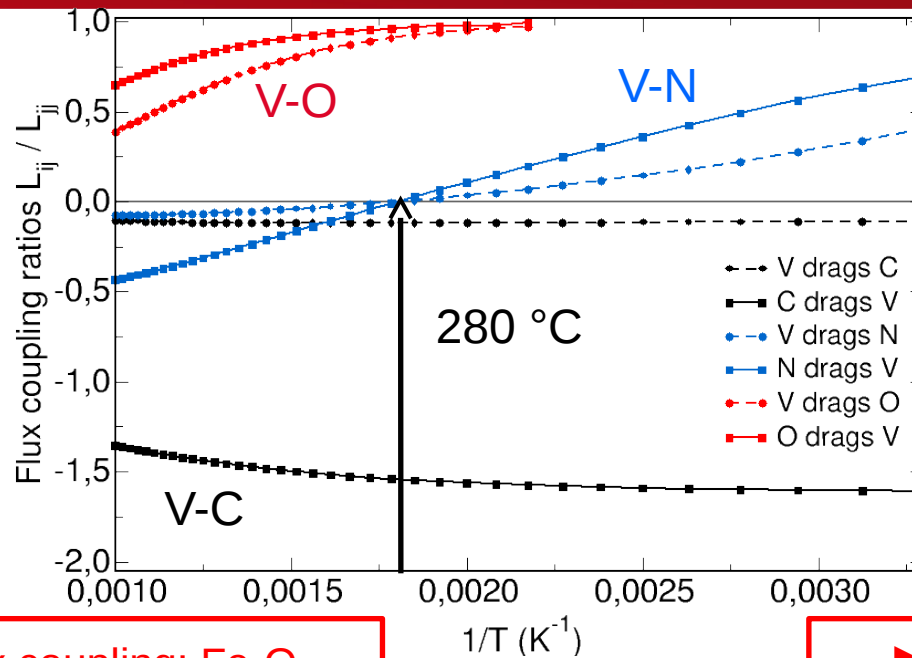
$$L_{\alpha\beta} = \sum_{c_i} [c_i] L_{\alpha\beta}^{eq}(c_i)$$

c_i : O, O2, O3, V, V2, V3,
VO, V2O, VO2, V3O

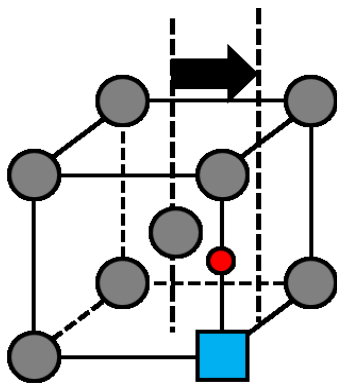


Flux coupling including paires VX

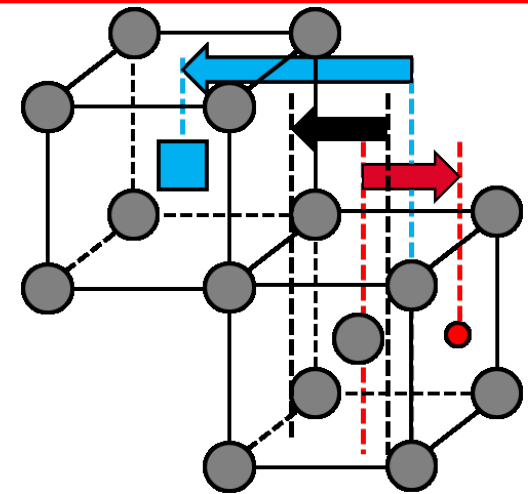
*T. Schuler & M. Nastar, PRB 93 (2016), 224101



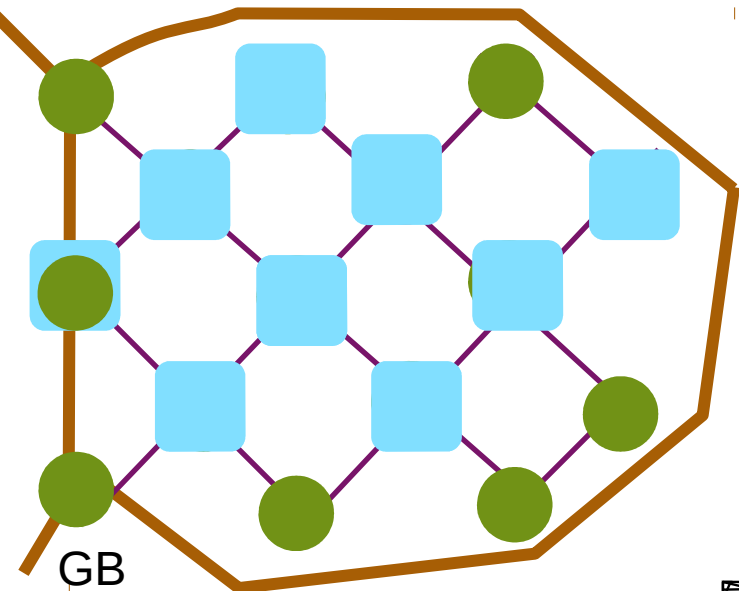
► Positive flux coupling: Fe-O
V drags O



► Negative flux coupling: Fe-C
V « repels » C



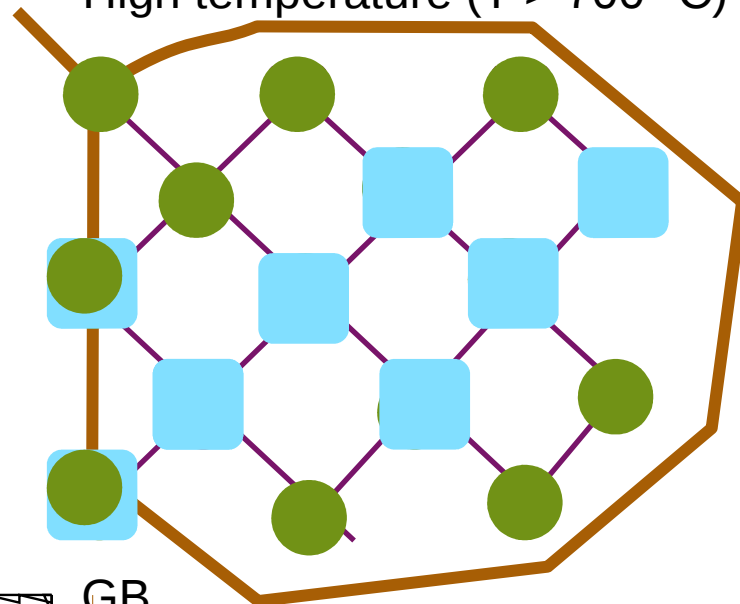
Low temperature ($T < 700\text{ °C}$)



← vacancy
← solute B

$G > 0$

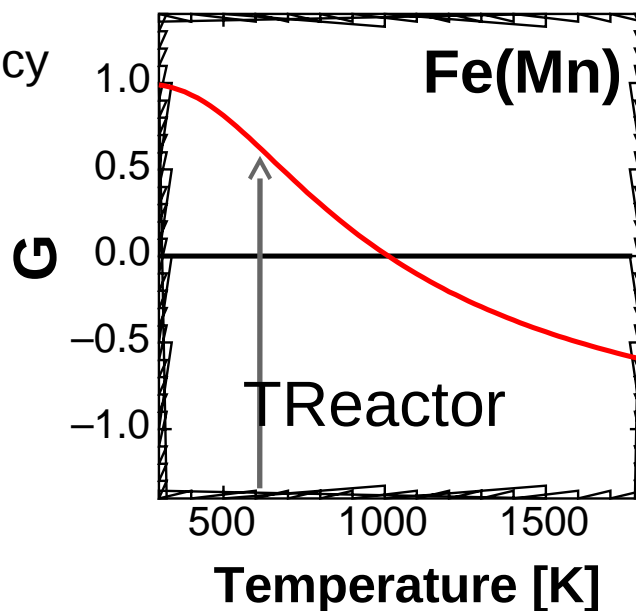
High temperature ($T > 700\text{ °C}$)



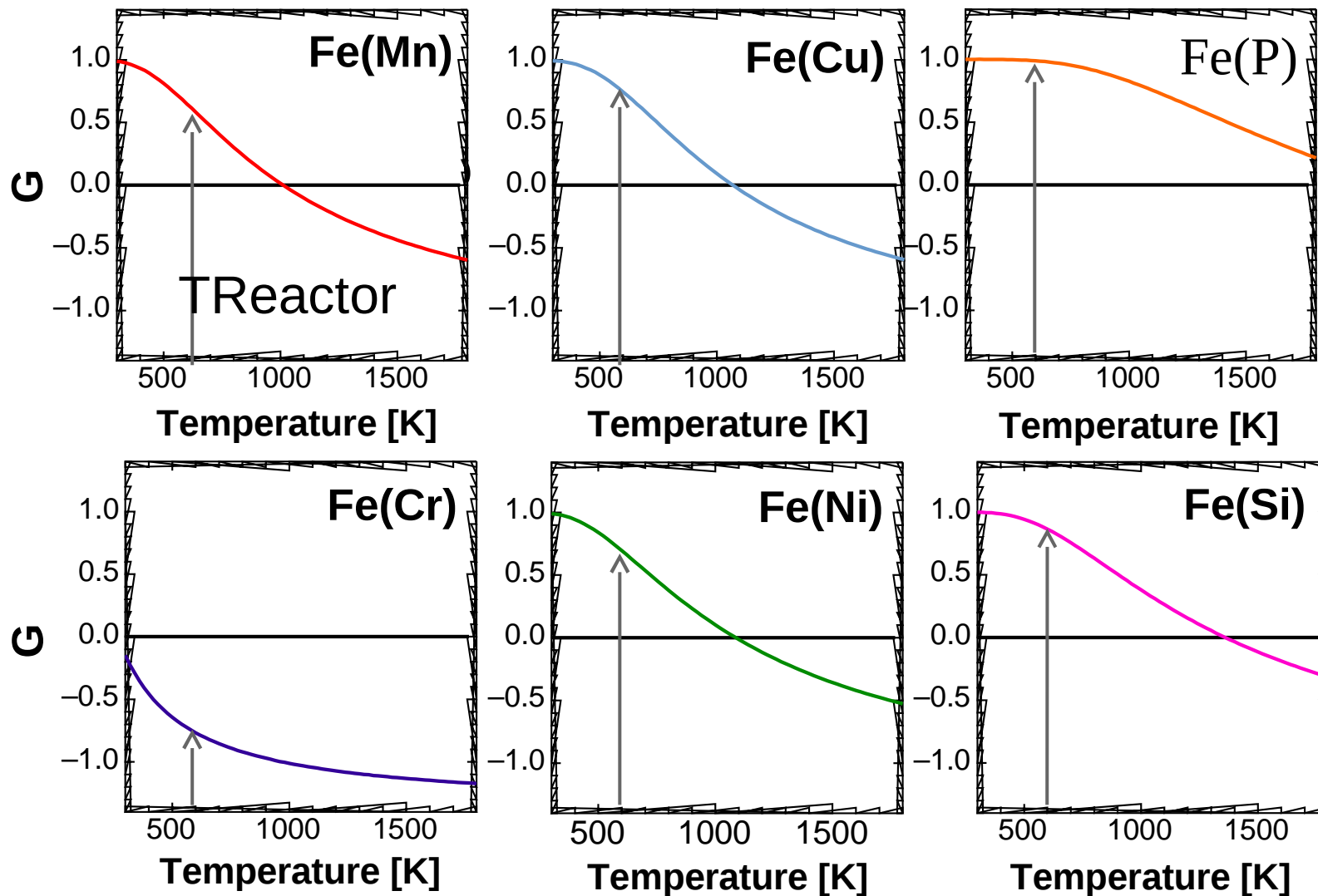
GB

← vacancy
→ solute B

$G < 0$



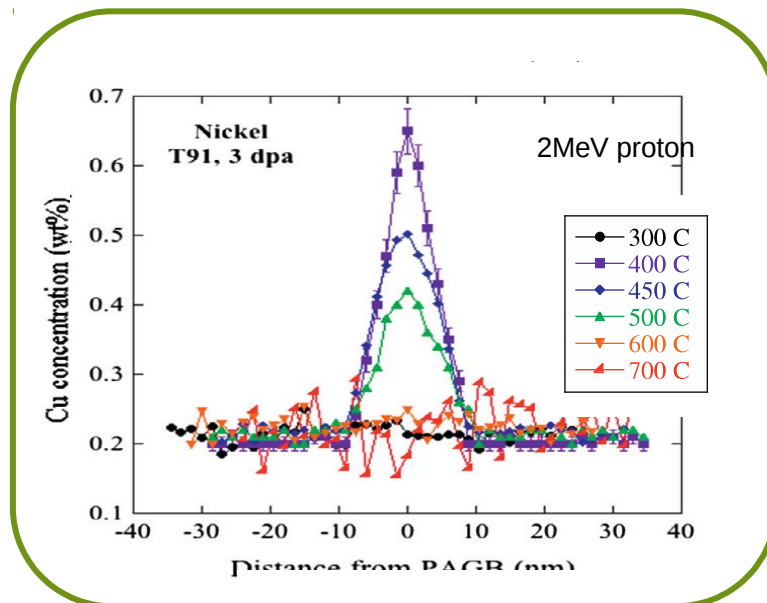
Vacancy flux coupling in Fe(X)



*L. Messina et al., Phys. Rev. B **90**, 104203 (2014).

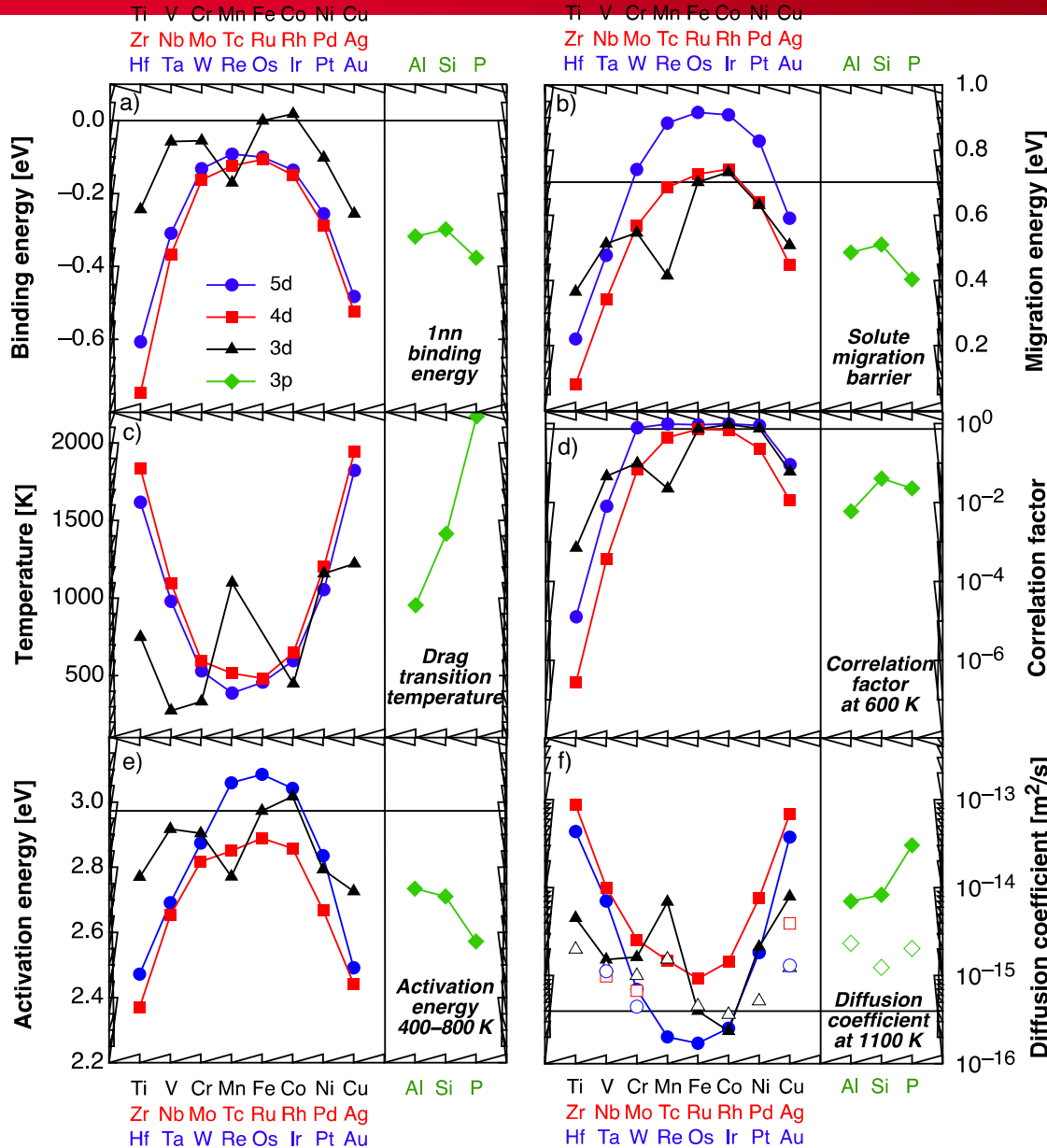
Minor element segregation in T91

*J.P. Wharry, G.S. Was, JNM 442 (2013) 7-16



- ✓ Enrichment of Ni, Si, Cu at grain-boundaries observed in T91 steels comforts the predicted solute drag by vacancy in the binary model alloys Fe (X = Ni, Si, Cu).
- ✓ Solute drag by vacancy might contribute to the formation of blooming phases (Cr, Ni, Si, P).

Systematic analysis of vacancy drag



- Extension to all transition-metal impurities.
- Identified common trends for wide range of properties.
- Impurity diffusion and flux coupling linked to electronic interactions between iron, impurities, and vacancies.
- Drag for all impurities! Even with repulsive solute-vacancy interactions.
- Electronic origin might suggest similar trends in other metals.

*L. Messina et al. PRB (2016)

✓ Dynamic Phase Diagrams of Fe-C, Fe-N and Fe-O

- Large increase of the solubility limit induced by stationary vacancy supersaturation
- VID is the dominant dissolution mechanism at intermediate irradiation flux and temperature against the ballistic mixing

✓ RIS in Fe-based alloys

○ Fe(C,O,N):

Positive flux coupling solute interstitials and vacancy except N at high T and C.
Non monotonous variation with T and vacancy supersaturation

○ Fe(substitutional X)

Vacancy: solute drag at $T < 700$ °C except Cr and solute depletion at high T

Thank you for your attention

This work was supported by

- the joint program "CPR ODISSEE" funded by AREVA, CEA, CNRS, EDF and Mécachrome under contract n° 070551.
- the Joint Programme on Nuclear Materials (JPNM) of the European Energy Research Alliance (EERA)
- The program IREMEV of the Euro-Fusion consortium